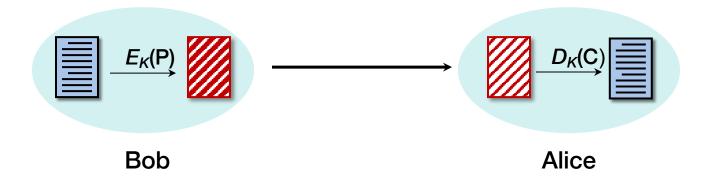


# Key Distribution

# Communicating with symmetric cryptography

- Both parties must agree on a secret key, K
- Message is encrypted, sent, decrypted at other side



#### Key distribution must be secret. Otherwise

- Messages can be decrypted by the adversary
- Users can be impersonated

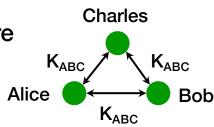
# Problems With Keys In Symmetric Cryptography

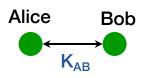
#### **Key Management**

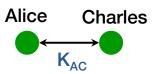
- Potentially a lot of keys to track
- Every communicating group of users needs a key

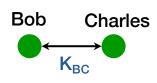
#### **Key Distribution**

- How do you communicate with someone you've never met?
- You cannot send them the secret key if the communication line is not secure









## Key Distribution

# Secure key distribution is the biggest problem with symmetric cryptography

# Key Exchange

## Trapdoor functions

#### **Trapdoor function**

- Easy to compute in one direction
- The inverse is difficult to compute without extra information

#### Example:

**96171919154952919** is the product of two prime #s. What are they?

But if you're told that one of them is 100225441

... then it's easy to compute the other: 959555959

## Example trapdoor functions

#### **Examples:**

#### **Factoring:**

pq = N EASY

find p,q given N DIFFICULT

Basis for RSA

#### **Discrete Log:**

 $a^b \mod c = N$  EASY

find b given a, c, N DIFFICULT

Basis for Diffie-Hellman & Elliptic Curve

"Difficult" = no known short-cuts; requires an exhaustive search

# Diffie-Hellman Key Exchange (DHKE)

#### Key distribution algorithm

- Allows two parties to share a secret key over a non-secure channel
- Not public key encryption
- Based on difficulty of computing discrete logarithms in a finite field compared with ease of calculating exponentiation

# Allows us to negotiate a secret common key without fear of eavesdroppers

- All arithmetic performed in a field of integers modulo some large number
- Both parties agree on
  - a large prime number p
  - and a **number**  $\alpha < p$
- Each party generates a public/private key pair

Private key for user  $i: X_i$ 

<u>Public</u> key for user *i*:  $Y_i = \alpha^{X_i} \mod p$ 

- Alice has secret key X<sub>A</sub>
- Alice sends Bob public key Y<sub>A</sub>
- Alice computes

$$K = Y_B^{X_A} \operatorname{mod} p$$

- Bob has secret key X<sub>B</sub>
- Bob sends Alice public key Y<sub>B</sub>

K = (Bob's public key) (Alice's private key) mod p

- Alice has secret key X<sub>A</sub>
- Alice sends Bob public key Y<sub>A</sub>
- Alice computes

$$K = Y_B^{X_A} \mod p$$

- Bob has secret key X<sub>B</sub>
- Bob sends Alice public key Y<sub>B</sub>
- Bob computes

$$K = Y_A^{X_B} \mod p$$

K' = (Alice's public key) (Bob's private key) mod p

- Alice has secret key X<sub>A</sub>
- Alice sends Bob public key Y<sub>A</sub>
- Alice computes

$$K = Y_B^{X_A} \mod p$$

expanding:

$$K = Y_B^{X_A} \mod p$$

$$= (\alpha^{X_B} \mod p)^{X_A} \mod p$$

$$= \alpha^{X_B X_A} \mod p$$

- Bob sends Alice public key Y<sub>B</sub>
- Bob computes

$$K = Y_A^{X_B} \mod p$$

expanding:

$$K = Y_B^{X_B} \mod p$$

$$= (\alpha^{X_A} \mod p)^{X_B} \mod p$$

$$= \alpha^{X_A X_B} \mod p$$

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$$K = K'$$

K is a common key, known only to Bob and Alice

### Diffie-Hellman simple example

Assume p=1151, 
$$\alpha$$
=57

- Alice's secret key  $X_A = 300$
- Alice's public key  $Y_A = 57^{300} \mod p = 282$
- Alice computes

$$K = Y_{R}^{X_{A}} \mod p = 1046^{300} \mod p$$

$$K = 105$$

- Bob's secret key  $X_B = 25$
- Bob's public key  $Y_B = 57^{25} \mod p = 1046$
- Bob computes

$$K = Y_A^{X_B} \mod p = 282^{25} \mod p$$

$$K = 105$$

Given p=1151,  $\alpha=57$ ,  $Y_A=282$ ,  $Y_B=1046$ , you cannot get 105

# Public Key Cryptography

# Public-key cryptography

#### Two related keys:

$$C = E_{K1}(P) \quad P = D_{K2}(C)$$

$$C' = E_{K2}(P) P = D_{K1}(C')$$
  $K_2$  is a private key

 $K_1$  is a public key  $K_2$  is a private key

#### **Examples:**

RSA,

Elliptic curve algorithms (ECC),

DSS (digital signature standard)

# RSA Public Key Cryptography

Ron Rivest, Adi Shamir, Leonard Adleman created the first public key encryption algorithm in 1977

#### Each user generates two keys:

Private key (kept secret)

Public key (can be shared with anyone)

#### Difficulty of algorithm based on the difficulty of factoring large numbers

Keys are functions of a pair of large (~600 digits) prime numbers

# RSA algorithm: key generation

- 1. Choose two random large prime numbers p, q
- 2. Compute the product n = pq and  $\phi(n) = (p 1)(q 1)$  n will be presented with the public & private keys. Length(n) is the **key length**
- 3. Choose the **public exponent**, e, such that:  $1 < e < \phi(n)$  and  $gcd(e, \phi(n)) = 1$ Choose a value where e and (p - 1)(q - 1) are relatively prime
- 4. Compute the **secret exponent**, *d* such that:

$$ed = 1 \mod \phi(n)$$
  
 $d = e^{-1} \mod ((p - 1) (q - 1))$ 

5. Public key = (e, n)Private key = (d, n)Discard  $p, q, \phi(n)$ 

#### You don't have to know this!

#### An example with small numbers

3, 11

$$(3-1) \times (11-1) = 20$$

Choose e=7

Find *d*: 
$$7d = 1 \mod 20$$
  
7 x 3 = 21  $\equiv 1 \mod 20$   
 $d = 3$ 

Pub key = 
$$(3, 33)$$
  
Pri key =  $(7, 33)$ 

# RSA Encryption

Key pair: public key = 
$$(e, n)$$
  
private key =  $(d, n)$ 

#### **Encrypt**

- Divide data into numerical blocks < n</li>
- Encrypt each block:

$$c = m^e \mod n$$

#### **Decrypt**

$$m = c^d \mod n$$

# RSA security

The security of RSA encryption rests on the difficulty of factoring a large integer

Public key = { modulus, exponent }, or {n, e}

- The modulus is the product of two primes, p, q
- The private key is derived from the same two primes

# RSA security

The security rests on the difficulty of factoring a large integer

```
Public key = { exponent, modulus }, or { e, n }
```

- The modulus is the product of two primes, p, q
- The private key is derived from the same two primes

If you know the public key (3, 33), can you derive the private key?

```
If you can factor 33 = 3 \times 11 \Rightarrow \phi(n) = 2 \times 11 = 20
Find d, such that 3d = 1 \mod 20
```

### **RSA Security**

Since the security of RSA rests on not knowing an efficient way to factor n = pq, we have to make it difficult to find factors via an exhaustive search

Common key lengths are 1024, 2048, 3072, 4096, 8129, 16384 bits

Example: a 2048-bit modulus (n) and secret exponent (d):

n =

0xa709e2f84ac0e21eb0caa018cf7f697f774e96f8115fc2359e9cf60b1dd8d4048d974cdf8422bef6be3c162b04b916f7ea2133f0 e3e4e0eee164859bd9c1e0ef0357c142f4f633b4add4aab86c8f8895cd33fbf4e024d9a3ad6be6267570b4a72d2c34354e0139e 74ada665a16a2611490debb8e131a6cffc7ef25e74240803dd71a4fcd953c988111b0aa9bbc4c57024fc5e8c4462ad9049c7f1a bed859c63455fa6d58b5cc34a3d3206ff74b9e96c336dbacf0cdd18ed0c66796ce00ab07f36b24cbe3342523fd8215a8e77f89e 86a08db911f237459388dee642dae7cb2644a03e71ed5c6fa5077cf4090fafa556048b536b879a88f628698f0c7b420c4b7

d =

0x10f22727e552e2c86ba06d7ed6de28326eef76d0128327cd64c5566368fdc1a9f740ad8dd221419a5550fc8c14b33fa9f058b9fa4044775aaf5c66a999a7da4d4fdb8141c25ee5294ea6a54331d045f25c9a5f7f47960acbae20fa27ab5669c80eaf235a1d0b1c22b8d750a191c0f0c9b3561aaa4934847101343920d84f24334d3af05fede0e355911c7db8b8de3bf435907c855c3d7eeede4f148df830b43dd360b43692239ac10e566f138fb4b30fb1af0603cfcf0cd8adf4349a0d0b93bf89804e7c2e24ca7615e51af66dccfdb71a1204e2107abbee4259f2cac917fafe3b029baf13c4dde7923c47ee3fec248390203a384b9eb773c154540c5196bce1

#### Each is 10617

# Weak RSA Public Keys

#### March 14, 2022

- Older software generated RSA keys that can be broken instantly with commodity hardware
- SafeZone library doesn't randomize the prime numbers well
  - Used to generate RSA keys
  - After selecting one prime #, the second one is in close proximity to the first
- Keys generated with primes that are too close together can be broken with Fermat's factorization method, described in 1643







REAKING KEYS —

#### Researcher uses 379-year-old algorithm to crack crypto keys found in the wild

It takes only a second to crack the handful of weak keys. Are there more out there?

DAN GOODIN - 3/14/2022, 5:31 PM



Cryptographic keys generated with older software now owned by technology company Rambus are weak enough to be broken instantly using commodity hardware, a researcher reported on Monday. This revelation is part of an investigation that also uncovered a handful of weak keys in the wild.

The software comes from a basic version of the SafeZone Crypto Libraries, which were developed by a company called Inside Secure and acquired by Rambus as part of its 2019 acquisition of Verimatrix, a Rambus representative said. That version was deprecated prior to the acquisition and is distinct from a FIPS-certified version that the company now sells under the Rambus FIPS Security Toolkit brand.

https://arstechnica.com/information-technology/2022/03/researcher-uses-600-year-old-algorithm-to-crack-crypto-keys-found-in-the-wild/

## Weak RSA Public Keys

- The product of two large primes can be written as N = (a b)(a + b)
  - where a is the middle between the two primes
  - b is the distance from the middle to each of the primes
- If the primes are close, then a is close to  $\sqrt{N}$
- Attack: guess a by starting from  $\sqrt{N}$  and then incrementing the guess
  - Calculate  $b^2 = a^2 N$
  - If the result is a square, then we guessed correctly
  - Calculate the factors p, q as p=a+b, q=a-b

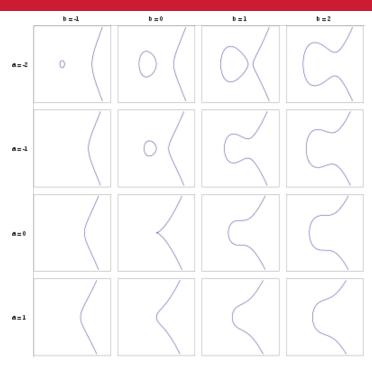
# Elliptic Curve Cryptography

# Key Generation Using discrete numbers, pick

- A prime number as a maximum (modulus)
- A curve equation in the family  $y^2 = x^3 + ax + b$
- A public base point on the curve, G
- A random private key, d
- Public key is computed from the private key, the base point, and the curve: d x G

#### To compute the private key from the public,

- We would need an elliptic curve **discrete logarithm** function
- This is difficult and is the basis for ECC's security



Catalog of elliptic curves https://en.wikipedia.org/wiki/Elliptic\_curve

# Elliptic Curve Cryptography

#### **Encryption**

#### Using a public key $Q_A$ and a message m

- G is the base point on the elliptic curve
- Map the message m to a point on the curve using a specified mapping function
  - *M* is the resulting point
- Choose a random integer k, where  $1 \le k \le n-1$  (where n is the order of the elliptic curve)
- Compute two points
  - $C_1 = k \times G$  this will be one part of the ciphertext
  - $C_2 = M + k \times Q_A$  this is the encrypted message
- Ciphertext =  $(C_1, C_2) = (k \times G, M + k \times Q_A)$

#### To compute the private key from the public,

- We would need an **elliptic curve discrete logarithm** function
- This is difficult and is the basis for ECC's security

#### ECC vs. RSA

#### RSA is still a widely used public key cryptosystem (but fading)

- Mostly due to inertia & widespread implementations it had a 27-year head start
- Trusted, well-tested deployments
- Trust in the algorithm
   (there was initial skepticism over the choice of curves and trust in the NIST, who approved them; the NSA tried to push an insecure random number generator)
- Simpler implementation

#### ECC offers higher security with fewer bits than RSA

- ECC is faster for key generation & encryption
  - The private key is any random number within a certain range (e.g., a 512-bit integer)
  - Encryption is about 10x faster than RSA
- Uses less memory
- NIST defines 15 standard curves for ECC
  - But many implementations support only a couple (P-256, P-384)

https://www.keylength.com/en/4/

http://https://www.enisa.europa.eu/publications/algorithms-key-size-and-parameters-report-2014

## Key length

#### Unlike symmetric cryptography, not every number is a valid key with RSA

#### Comparable complexity:

- 3072-bit RSA = 256-bit elliptic curve = 128-bit symmetric cipher
- 15360-bit RSA = 512-bit elliptic curve = 256-bit symmetric cipher

#### Recommendations for long-term security

The European Union Agency for Network and Information Security (ENISA) and the National Institute for Science & Technology (NIST) recommend:

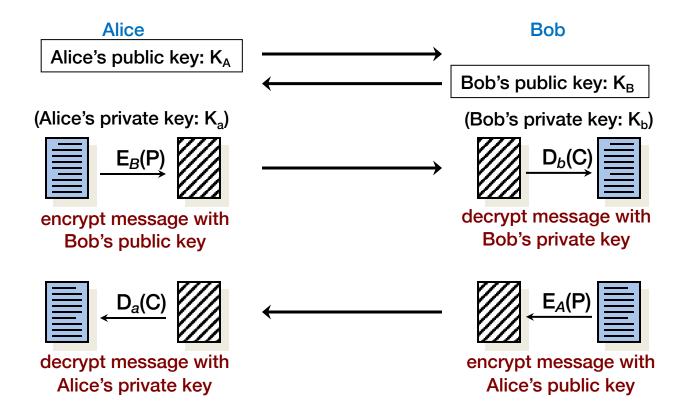
AES: 256-bit keys RSA: 15,360-bit keys ECC: 512 bit-keys

# Communication with public key algorithms

#### Different keys for encrypting and decrypting

No need to worry about key distribution

## Communication with public key algorithms



#### Public key algorithms are not used for communication

Calculations are very expensive relative to symmetric algorithms Speeds on an M1 Mac Mini\*:

Algorithm	bytes/sec
AES-128-CBC	1,538,484,000
AES-256-CBC	1,097,739,000
RSA-2048 encrypt	56,225,434
RSA-2048 decrypt	2,695,014
RSA-4096 encrypt	9,805,875
RSA-4096 decrypt	143,053

AES: ~7600x faster to decrypt; 100x faster to encrypt than RSA

#### Public key algorithms are not used for communication

#### Vulnerability to known plaintext attacks (or guessing)

- Content must be broken into smaller blocks since each block is treated like a number. An attacker can
  encrypt a wide set of predicted content with the recipient's public key and then look for matches in the
  ciphertext.
  - If I send "Yes" to you, I need to encrypt it with your public key. The attacker can encrypt "Yes", "No", and any other
    expected content with that same public key and see what matches the content I send. If there's a predicted chunk of
    a message, the attacker can spot it.

#### Some algebraic relationships may be preserved

Some algebraic relationships that exist between plaintext content may exist with public key algorithms.
 This can provide an attacker with insights on the relationship between content

#### ECC is faster than RSA and uses shorter keys

- ECC public key generation is efficient compared with RSA but still But is still much slower than symmetric algorithms and not considered secure for bulk data
- Encrypt messages n bits long with an n-bit elliptic curve, but the output can be 2n bits long
- requires math (point multiplication): see <a href="https://en.wikipedia.org/wiki/Elliptic\_curve\_point\_multiplication">https://en.wikipedia.org/wiki/Elliptic\_curve\_point\_multiplication</a>

# Hybrid Cryptosystems

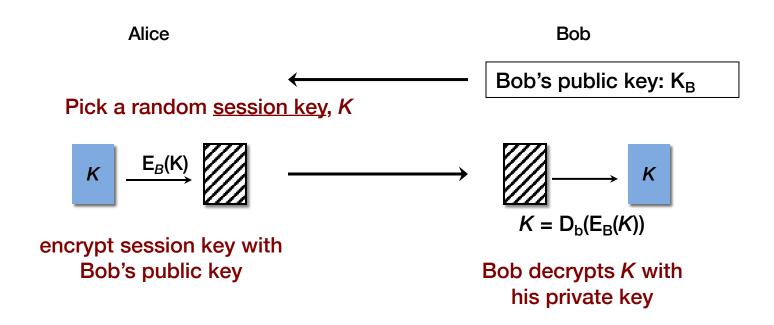
## Hybrid Cryptosystems

- Session key: randomly-generated symmetric key for one communication session
- Use a public key algorithm to send the session key
- Use a symmetric algorithm to encrypt data with the session key

#### Public key algorithms are never used to encrypt messages

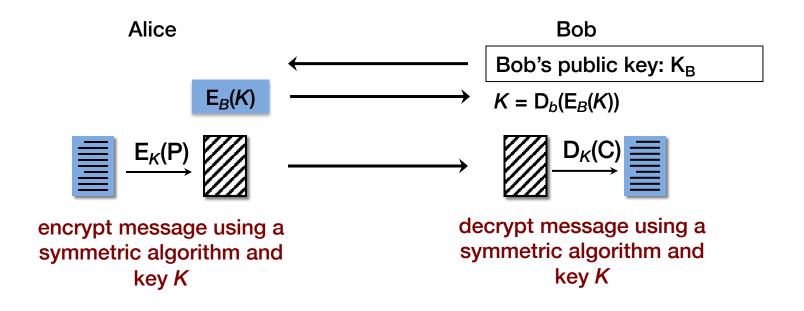
- MUCH slower; vulnerable to chosen-plaintext and algebraic attacks

## Communication with a hybrid cryptosystem

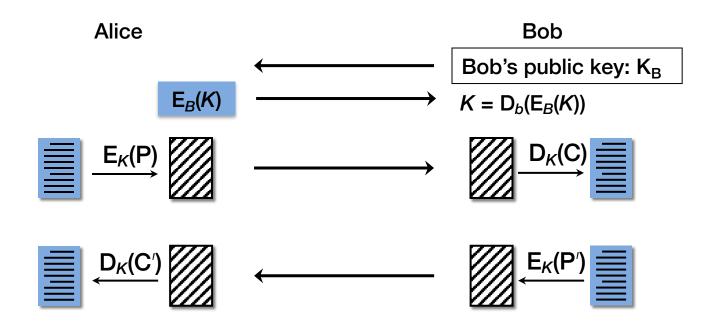


Now Bob knows the secret session key, K

## Communication with a hybrid cryptosystem



## Communication with a hybrid cryptosystem



decrypt message using a symmetric algorithm and key *K* 

encrypt message using a symmetric algorithm and key *K* 

# Forward Secrecy

## Private keys need to be protected

Pick a session key & Bob decrypts the session key with his private key

## Suppose an attacker steals Bob's private key

- Future messages can be compromised
- The attacker can also go through past messages & decrypt old session keys

## Security rests entirely on the secrecy of Bob's private key

If Bob's private key is compromised, all recorded past traffic can be decrypted

## Forward Secrecy

## Forward secrecy

- Compromise of long-term keys does not compromise past session keys
- There is no one secret to steal that will compromise multiple messages

## Achieving Forward Secrecy

#### Use <u>ephemeral keys</u> for key exchange + <u>session keys</u> for communication

#### Diffie-Hellman key exchange is commonly used for key exchange

- Generate a set of keys per session
- Use the derived common key as the encryption/decryption key ... or as a key to encrypt a session key
- Not recoverable as long as private keys are thrown away
   Unlike RSA keys, key generation in Diffie-Hellman is extremely efficient

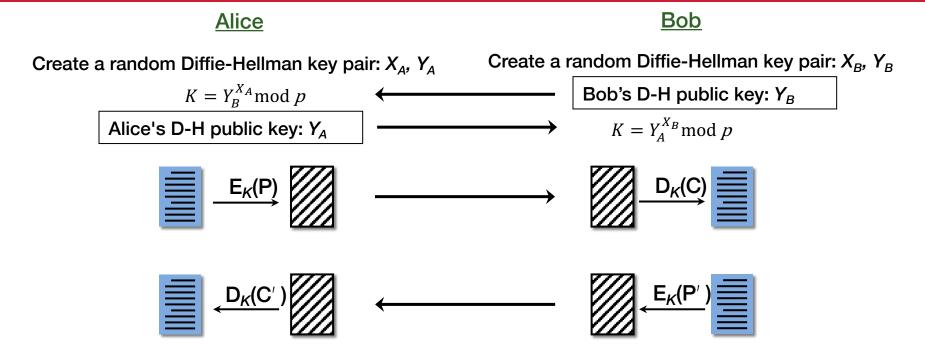
#### **Ephemeral** = single-use keys

Client & server will generate new Diffie-Hellman parameters for each session – all will be thrown away after the session

Diffie-Hellman is preferred over RSA for key exchange to achieve forward secrecy. Generating Diffie-Hellman keys is a rapid, low-overhead process.

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## Communication with a hybrid cryptosystem (DHKE)



decrypt message using a symmetric algorithm and key *K* 

encrypt message using a symmetric algorithm and key *K* 

## Cryptographic systems: summary

#### Symmetric ciphers

Based on SP-networks (usually) = substitution & permutation sequences

#### Asymmetric ciphers – public key cryptosystems

 Based on trapdoor functions: easy to compute in one direction, difficult to compute in the other direction without special information (the trapdoor)

#### Hybrid cryptosystem

- Pick a random session key + public key algorithm for key exchange
- Use a symmetric key algorithm to encrypt traffic back & forth
- Forward secrecy: establish session key via ephemeral keys

#### Key exchange algorithms (more to come later)

- Diffie-Hellman
- Public key

Enables secure communication without knowledge of a shared secret

#### Perfect secrecy

Ephemeral keys + Session key

# Looking ahead

## RSA cryptography in the future

- Based on the difficulty of factoring products of two large primes
- Factoring algorithms get more efficient as numbers get larger
  - As the ability to decrypt numbers increases, the key size must therefore grow even faster
  - This is not sustainable (especially for embedded devices)
- ECC is a better choice for most applications

## Quantum Computers & Cryptography

# Once (if) useful quantum computers can be built, they will be able to:

## Factor efficiently

- Shor's algorithm factors numbers exponentially faster
- RSA will not be secure anymore
- Find discrete logarithms & elliptic curve discrete logarithms efficiently
  - Diffie-Hellman key exchange & ECC will not be secure



## Not all is bad

# Symmetric cryptography is largely immune to attacks

Some optimizations are predicted (Grover's algorithm):

Crack a symmetric cipher in time proportional to the square root of the key space size:  $2^{n/2}$  vs.  $2^n$ 

-The recommendation is to use 256-bit AES to be safe



## Quantum-proofing cryptography

## Quantum computing is not faster at everything

Only four types of problems are currently identified where quantum computing offers an advantage

Researchers have been developing algorithms that are be made more efficient with quantum computing

31108953 1190018662 104910828 2598220447 3027417464 3006531459 2376520867 804531264 2430217482 1122428373 Example: Add 3 out of a set of 10 numbers

- Give the sum to a friend and ask them to determine which numbers were added
- Try this if someone picks 500 out of 1,000 numbers with 1,000 digits each

Which 3 numbers add up to 5656746864?

https://www.scientificamerican.com/article/new-encryption-system-protects-data-from-quantum-computers/

## NSA Releases First 3 Post-Quantum Encryption Standards

2016: NSA called for a migration to "post-quantum cryptographic algorithms"

July 2020: Narrowed submissions down to 7 finalists & 8 alternates

August 13, 2024: Releases first set of standards

#### Solution families

- Lattice-based
- 2. Code-based
- 3. Multivariate

# Message Integrity

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## McCarthy's Spy Puzzle (1958)

## The setting:

- Two countries are at war
- One country sends spies to the other country
- To return safely, spies must give the border guards a password

#### **Conditions**

- Spies can be trusted
- Guards chat information given to them may leak

## McCarthy's Spy Puzzle

## Challenge

- How can a border guard authenticate a person without knowing the password?
- Enemies cannot use the guard's knowledge to introduce their own spies

## Solution to McCarthy's puzzle

## Michael Rabin, 1958

- Use a one-way function, B = f (A)
  - Guards get B
    - Enemy cannot compute A if they know A
  - Spies give A, guards compute f(A)
    - If the result is B, the password is correct.

## Example function:

- Middle squares
  - Take a 100-digit number (A), and square it
  - Let B = middle 100 digits of 200-digit result

## Example of a one-way function: middle squares

Example with a 20-digit number

A = 18932442986094014771

 $A^2 = 358437397421700454779607531189166182441$ 

Middle square, B = 42170045477960753118

Given A, it is easy to compute B

Given B, it is difficult to compute A

"Difficult" = no known short-cuts; requires an exhaustive search

## Cryptographic hash functions

## Cryptographic hash functions

## **Properties**

- Arbitrary length input → fixed-length output
- Deterministic: you always get the same hash for the same message
- One-way function (pre-image resistance, or hiding)
  - Given H, it should be difficult to find M such that H=hash(M)
- Collision resistant
  - Infeasible to find any two different strings that hash to the same value:
     Find M, M' such that hash(M) = hash(M')
- Output should not give any information about any of the input
  - Like cryptographic algorithms, relies on diffusion
- Efficient
  - Computing a hash function should be computationally efficient

Also called *digests* or *fingerprints* 

## Hash functions are the basis of integrity

- Not encryption
- Can help us to detect:
  - Masquerading:
    - Insertion of message from a fraudulent source
  - Content modification:
    - Changing the content of a message
  - Sequence modification:
    - Inserting, deleting, or rearranging parts of a message
  - Replay attacks:
    - Replaying valid sessions

## Hash Algorithms

#### Use iterative structure like block ciphers do ... but use no key

#### Example:

- Secure Hash Algorithm, SHA-1
  - Designed by the NSA in 1993; revised in 1995
  - Used in the NIST Digital Signature Standard (DSS)
  - Produces 160-bit hash values
  - Chosen prefix collision attacks were demonstrated in May 2019

#### Successors

- SHA-2 (2001) SHA-256, SHA-384, SHA-512
  - Produces 224, 256, 384, or 512-bit hashes
  - Approved for use with the NIST Digital Signature Standard (DSS)
- **SHA-3** (2015)
  - Can be substituted for SHA-2
  - Improved robustness

## Example: SHA-1 Overview

#### Prepare the message

- Append the bit 1 to the message
- Pad message with 0 bits so its length = 448 mod 512
- Append length of message as a 64-bit big endian integer

## Use an Initialization Vector (IV) = 5-word (160-bit) buffer:

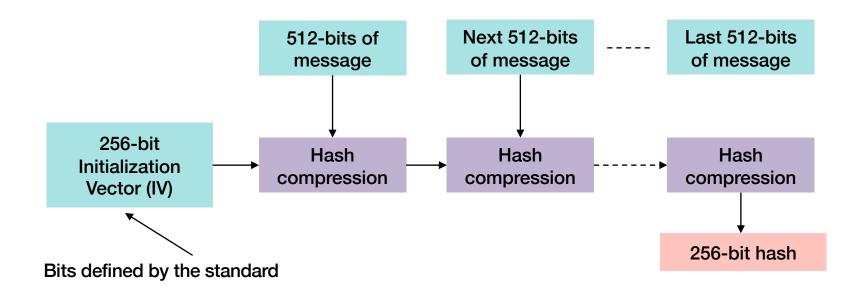
```
a = 0x67452301 b = 0xefcdab89 c = 0x98badcfe
d = 0x10325476 e = 0xc3d2e1f0
```

## Process the message in 512-bit chunks

- Expand the 16 32-bit words into 80 32-bit words via XORs & shifts
- Iterate 80 times to create a hash for this chunk
  - Various sets of ORs, XORs, ANDs, shifts, and adds
- Add this hash chunk to the result so far

See https://www.saylor.org/site/wp-content/uploads/2012/07/SHA-1-1.pdf

## SHA-2 Overview



## Popular (& formerly popular) Hash Functions

#### MD5

- 128 bits
- Linux passwords used to use this
- · Rarely used now since weaknesses were found
- 160 bits was widely used: still used as a checksum in Git & torrents
- Google demonstrated a collision attack in Feb 2017

#### SHA-1

- ... Google had to run >9 quintillion SHA-1 computations to complete the attack
- ... but already being phased out since weaknesses were found earlier
- Used for message integrity in GitHub

#### Believed to be secure

#### Designed by the NSA; published by NIST

- **SHA-2** Variations: SHA-224, SHA-256, SHA-384, SHA-512
  - Linux passwords use SHA-512
  - Bitcoin uses SHA-256

#### SHA-3

#### Believed to be secure

256 & 512 bit

#### Believed to be secure

Designed to be slow!

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Believed to be secure

#### bcrypt

- Blowfish cipher used for bcrypt password hashing in OpenBSD since 1997
- Phased out in 2023: scrypt and Argon2 are replacements

Linux passwords used to use this

September 22, 2024 CS 419 © 2024 Paul Krzyzanowski

## Creating hashes via the openssl command

#### MD5 hash

```
echo 'hello, world!'| openssl dgst -md5
MD5(stdin)= 910c8bc73110b0cd1bc5d2bcae782511
```

#### SHA-1 hash

```
echo 'hello, world!'| openssl dgst -sha1
SHA1(stdin)= e91ba0972b9055187fa2efa8b5c156f487a8293a
```

#### 256-bit SHA-2 hash

```
echo "hello, world!" | openssl dgst -sha2-256
SHA2-256(stdin)= 4dca0fd5f424a31b03ab807cbae77eb32bf2d089eed1cee154b3afed458de0dc
```

#### 256-bit SHA-3 hash

```
echo "hello, world!" | openssl dgst -sha3-256
SHA3-256(stdin)= 5208fd28810f11b7781a86289fb9121ccc754a5bd8260bcfa539163890092c7e
```

#### 512-bit SHA-3 hash

```
echo "hello, world!" | openssl dgst -sha3-512

SHA3-512(stdin)=

8fc33b84ff22559082893fdc73f6877e590eb67533441fe5e48cd6d8a11aaf8d6270f82ef437c2c758000d65b09b4511

6b9c0eb3f3162149b13ca98c8cc8c90f
```

## Hash Collisions

## Hashes are *collision resistant*, but collisions can occur

## Pigeonhole principle

- If you have 10 pigeons & 9 compartments, at least one compartment will have more than one pigeon
- A hash is a fixed-size small number of bits (e.g., 256 bits = 32 bytes)
- Every possible permutation of an arbitrary number of bytes cannot fit into every permutation of 32 bytes!



wikipedia

## Collisions: The Birthday Paradox

How many people need to be in a room such that the probability that two people will have the same birthday is > 0.5?

## Your guess before you took a probability course: 183

This is true to the question of "how many people need to be in a room for the probability that someone else will have the same birthday as *one specific student*?"

Answer: 23

$$p(n) = 1 - \frac{n! \cdot \binom{365}{n}}{365^n}$$

Approximate solution for # people required to have a 0.5 chance of a shared birthday, where m = # days in a year

$$n \approx \sqrt{2 \times m \times 0.5}$$

## The Birthday Paradox: Implications

 Searching for a collision with a pre-image (known message) is A LOT harder than searching for two messages that have the same hash

- Strength of a hash function is approximately ½ (# bits)
  - 256-bit hash function has a strength of approximately 128 bits
  - But that's a huge space!

$$2^{128} = 3.4 \times 10^{38}$$

- It's not feasible to try that many messages in the hope of finding a collision
  - BTW ... the odds of winning the Powerball lottery are only 1:2.9×10<sup>8</sup>

# Data Integrity: Message Authentication Codes and Digital Signatures

## Data Integrity

## How do we detect that a message has been tampered?

- A cryptographic hash acts as a checksum
- Associate a hash with a message
  - We're not encrypting the message
  - We're concerned with *integrity*, not *confidentiality*
- If two messages hash to different values, we are convinced that the messages are different

$$H(M) \neq H(M')$$

## MACs (also called a Keyed Hash)

We rely on hashes to assert the integrity of messages

But an attacker can create a new message & a new hash and replace H(M) with H(M')

So, let's create a checksum that <u>relies on a key for validation</u>

Message Authentication Code (MAC)

Two forms: hash-based & block cipher-based

## HMAC: Hash-based MAC

## We can create a MAC from a cryptographic hash function

HMAC = Hash-based Message Authentication Code

 $HMAC(m, k) = H((opad \oplus k) || H(ipad \oplus k) || m))$ 

#### where

*H* = cryptographic hash function

*opad* = outer padding 0x5c5c5c5c ... (01011100...)

*ipad* = inner padding 0x36363636... (00110110...)

**k** = secret key

*m* = message

⊕ = XOR, | = concatenation

Note the extra hash.

The simple form of an HMAC would simply be hash(m, k)

The HMAC standard devised this to strengthen the HMAC against weaker hash functions.

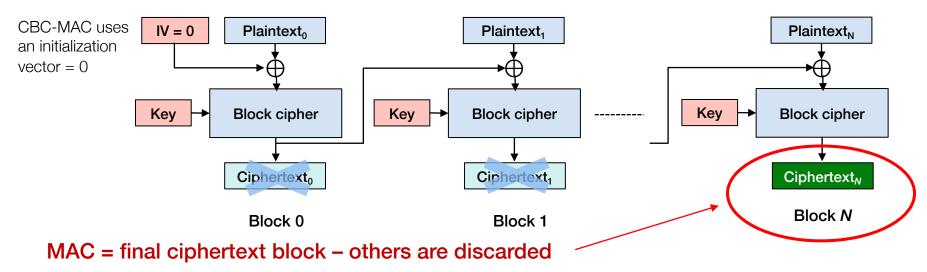
Basically, incorporate a key into the message before hashing it

See RFC 2104

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## Block Cipher Based MAC: CBC-MAC

Cipher Block Chaining (CBC) ensures that every encrypted block is a function of all previous blocks



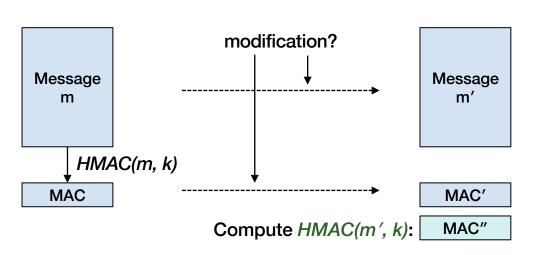
Examples: AES-CBC-MAC, DES-MAC

Don't use the same key for the MAC as for encrypting the message

If an adversary gets one of the keys, she will be unable to create either a valid message or a valid hash

## Using a MAC

Alice  $\longleftarrow$  Both have the shared key,  $k \longrightarrow$  Bob



- 1. Bob receives the Message m' and a MAC.
- 2. Knowing the key, k, he generates a MAC for the message: MAC" = HMAC(m', k)
- 3. If MAC' = MAC", he's convinced that the message has not been modified

## Digital Signatures

## MACs rely on a shared key

Anyone with the key can modify and re-sign a message

## Digital signature properties

- Only you can sign a message, but anyone can validate it
- You cannot cut and paste the signature from one message to another
- If the message is modified, the signature will be invalid
- An adversary cannot forge a signature
  - Even after inspecting an arbitrary number of signed messages

# Digital Signature Primitives

### 1. Key generation

```
{ secret_key, verification_key } := gen_keys(key_size)
```

### 2. Signing

```
signature := sign(message, secret_key)
```

#### 3. Validation

```
Isvalid := verify(verification_key, message, signature)
```

### We sign *hash(message)* instead of the *message*

- We'd like the signature to be a small, fixed size
- We may not need to hide the contents of the message
- We trust hashes to be collision-free

# Digital Signatures & Public Key Cryptography

### Public key cryptography enables digital signatures

Alice encrypts a message with her private key

$$S = E_a(M)$$

Anyone can decrypt it using her public key

$$D_A(S) = D_A(E_a(M)) = M$$

Nobody but Alice can create S

# Popular Digital Signature Algorithms

Digital Signature Algorithms combine hashing + encryption into one step

```
signature: S := E_{pri\_key}(H(M))
verification = H(M) \stackrel{?}{=} D_{pub\_key}(S)
```

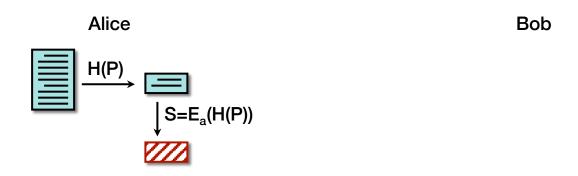
- DSA: Digital Signature Algorithm
  - NIST standard Uses SHA-1 or SHA-2 hash
  - Key pair based on difficulty of computing discrete logarithms
- ECDSA: Elliptic Curve Digital Signature Algorithm
  - Variants of DSA that uses elliptic curve cryptography
  - Used in bitcoin
- EdDSA: Edwards-curve Digital Signature Algorithm
  - Slightly faster than ECDSA

# Digital signatures



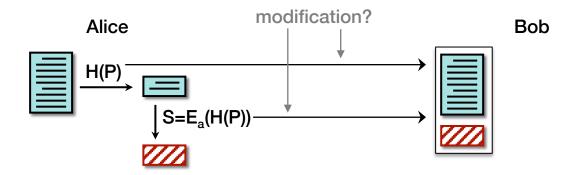
Alice generates a hash of the message, H(P)

## Digital signatures: public key cryptography



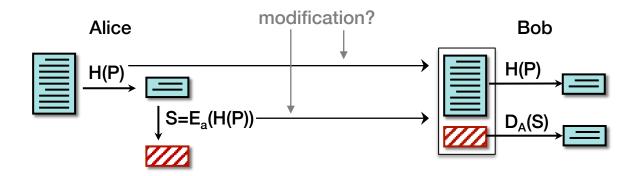
Alice encrypts the hash with her private key
This is her signature.

# Using Digital Signatures



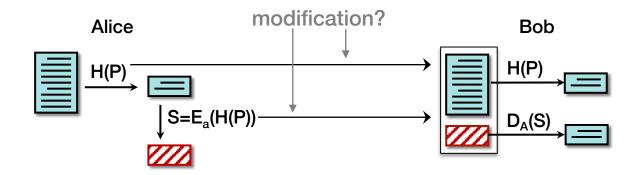
Alice sends Bob the message & the encrypted hash

# Using Digital Signatures



- 1. Bob decrypts the hash using Alice's public key
- 2. Bob computes the hash of the message sent by Alice

# Using Digital Signatures



If the hashes match, the signature is valid ⇒ the encrypted hash *must* have been generated by Alice

# Digital signatures & non-repudiation

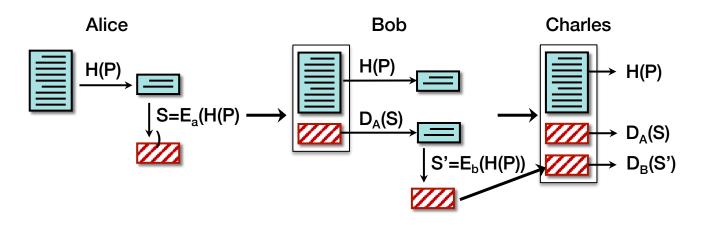
### Digital signatures provide non-repudiation

 Only Alice could have created the signature because only Alice has her private key

### Proof of integrity

- The hash assures us that the original message has not been modified
- The encryption of the hash assures us that an attacker could not have re-created the hash

## Digital signatures: multiple signers



#### **Charles:**

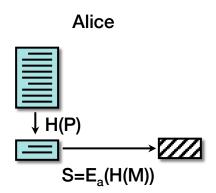
- Generates a hash of the message, H(P)
- Decrypts Alice's signature with Alice's public key
  - Validates the signature: D<sub>A</sub>(S) <sup>2</sup> H(P)
- Decrypts Bob's signature with Bob's public key
  - Validates the signature: D<sub>B</sub>(S) <sup>2</sup> H(P)

### If we want to keep the message secret

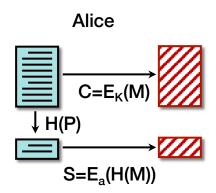
combine encryption with a digital signature

### Use a session key:

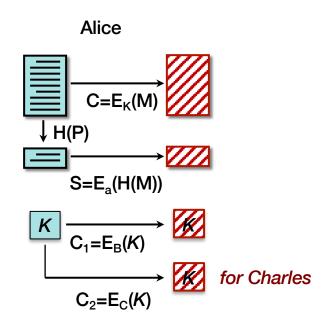
- Pick a random key, K, to encrypt the message with a symmetric algorithm
- Encrypt K with the public key of each recipient
- For signing, encrypt the hash of the message with sender's private key



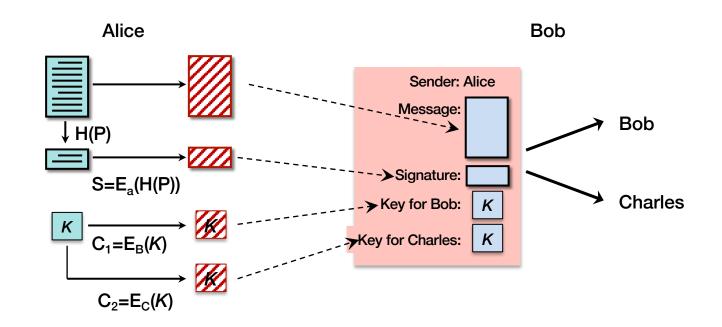
Alice generates a digital signature by encrypting the message with her private key



Alice picks a random key, *K*, and encrypts the message *P* with it using a symmetric cipher



Alice encrypts the session key for each recipient of this message using their public keys



### The aggregate message is sent to Bob & Charles

Note: we do not have forward secrecy by doing this

# Certificates: Identity Binding

## Public Keys as Identities

- A public signature verification key can be treated as an identity
  - Only the owner of the corresponding private key will be able to create the signature
- New identities can be created by generating new random {private, public} key pairs

- Anonymous identity no identity management
  - A user is known by a random-looking public key
  - Anybody can create a new identity at any time
  - Anybody can create as many identities as they want
  - A user can throw away an identity when it is no longer needed
  - Example: your Bitcoin identity = hash(public key)

# Identity Binding

- How does Alice know Bob's public key is really his?
- Get it from a trusted server?
  - What if the enemy tampers with the server?
  - Or intercepts Alice's query to the server (or the reply)?
  - What set of public keys does the server manage?
  - How do you find it in a trustworthy manner?

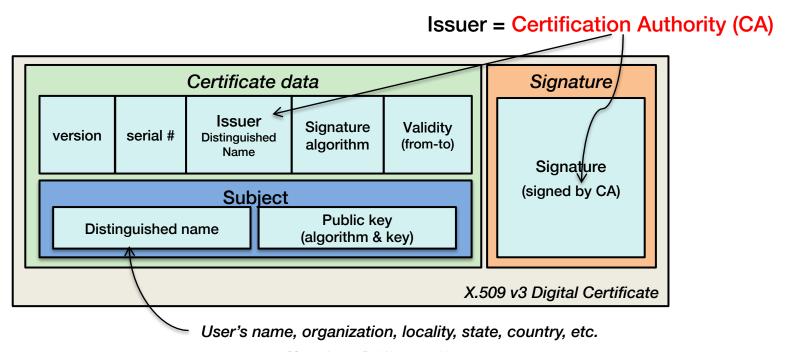
# Identity Binding – Another Option

- Have a trusted party sign Bob's public key
- Once signed, it is tamper-proof
  - An attacker cannot generate the signature after modifying the key
- But we need to know it's Bob's public key and who signed it
  - Create & sign a data structure that
    - Identifies Bob
    - Contains his public key
    - Identifies who is doing the signing

### X.509 Certificates

### ISO introduced a set of authentication protocols

X.509: Structure for public key certificates:

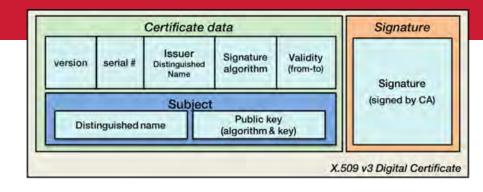


### X.509 Certificates

### To validate a certificate

Verify its signature:

- 1. Get the issuer (CA) from the certificate
- 2. Validate the certificate's signature against the issuer's public key
  - Hash contents of certificate data
  - Decrypt CA's signature with <u>CA's public key</u>



### Obtain CA's public key (certificate) from trusted source

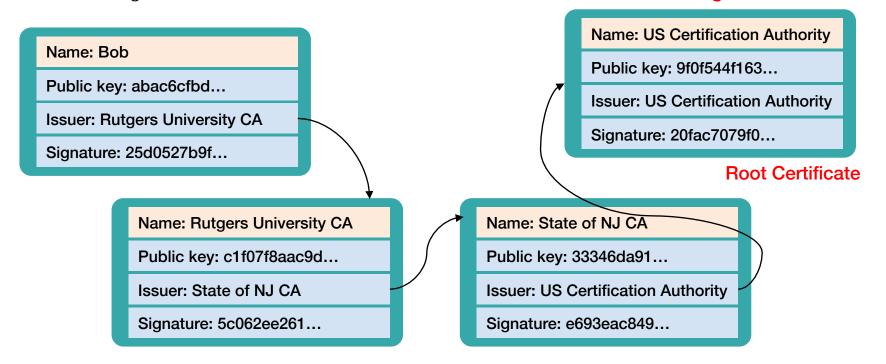
Certificates prevent someone from using a phony public key to masquerade as another person

...if you trust the CA

# Certification Authorities (CAs)

### How do you know the public key of the CA?

You can get it from another certificate! ⇒ this is called certificate chaining



# Certification Authorities (CAs)

- But trust must start somewhere
   You need a public key you can trust this is the root certificate
  - Apple's Trust Store is pre-loaded with over 160 CA certificates
    - Stores non-personal security info; accessed via Keychain
  - Windows stores them in the Certificate Store and makes them accessible via the Microsoft Management Console (mmc)
  - Android stores them in Credential Storage

### Can you trust a CA?

- Maybe...
   check their reputation and read their Certification Practice Statement (CPS)
- Even trustworthy ones might get hacked (e.g., VeriSign in 2010)

### Key revocation

### Used to invalidate certificates before expiration time

- Usually because of a compromised key
- Or policy changes (e.g., someone leaves a company)

### Certificate revocation list (CRL)

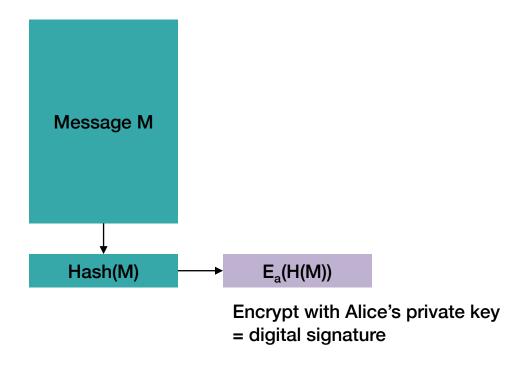
- Lists certificates that are revoked
- Only certificate issuer can revoke a certificate

#### Problems

- Need to make sure that the entity issuing the revocation is authorized to do this
- Revocation information may not circulate quickly enough
  - Dependent on dissemination mechanisms, network delays & infrastructure
- Some systems may not have been coded to process revocations

# Code Integrity

## Review: signed messages



## We can sign code as well

### Validate integrity of the code

If the signature matches, then the code has not been modified

### Enables

- Distribution from untrusted sources
- Distribution over untrusted channels
- Detection of modifications by malware

### Signature = encrypted hash signed by trusted source

Does <u>not</u> validate the code is good ... just where it comes from

# Code Integrity: signed software

### Windows since XP\*: Microsoft Authenticode

- SignTool command
- Hashes stored in system catalog or signed & embedded in the file
- Microsoft-tested drivers are signed

### macOS

- codesign command
- Hashes & certificate chain stored in file

### Also Android & iOS

## Code signing: Microsoft Authenticode

A format for signing executable code (dll, exe, cab, ocx, class files)

### Software publisher:

- Generate a public/private key pair
- Get a digital certificate from a certification authority (CA) that is enrolled in the Microsoft Trusted Root Certificate Program
- Generate a hash of the code to create a fixed-length digest
- Encrypt the hash with your private key
- Combine digest & certificate into a Signature Block
- Embed Signature Block in executable package

#### Microsoft SmartScreen:

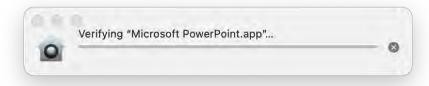
Manages reputation based on download history, popularity, anti-virus results

### Recipient:

- Call WinVerifyTrust function to validate:
  - Validate certificate, decrypt digest, compare with hash of downloaded code

# Per-page hashses

Integrity check when program is first loaded (this takes time)



- Check a hash for a page when it is needed (demand paging)
  - This is efficient (pages are small; checking a hash is quick)

Per-page hashes can be disabled optionally on both Windows and macOS

# Windows code integrity checks

- Implemented as a file system driver
  - Works with demand paging from executable
  - Check hashes for every page as the page is loaded
- Hashes stored in system catalog or embedded in file along with X.509 certificate
- Check integrity of boot process
  - Kernel code must be signed or it won't load
  - Drivers shipped with Windows must be certified or contain a certificate from Microsoft

# The End